

MAHARISHI VEDVYAS GOVT P.G. COLLEGE, BHAKHARA (C.G.)

MATHEMATICS

ASSIGNMENT -2020

PAPER THIRD

(VECTOR ANALYSIS AND GEOMETRY)

B.Sc. I Year (REGULAR)

TIME: 3 Hours

M.M.: 50

Note: Answer any five questions. Each question carries equal marks.

1. a) Define gradient. (4 + 6=10)

b) If a, b, c are three non-coplanar vectors, then show that $[a \times b, b \times c, ca] = [a b c]^2$

2. a) State Green's theorem. (4 + 6=10)

b) Use Green's theorem in plane to evaluate $I = \oint_C [(x + 2y)dx + (y + 3x)dy]$,

where C is the circle $x^2 + y^2 = 1$.

3. a) Define confocal conics. (4 + 6=10)

b) Prove that confocal conics cut at right angles.

4. a) State Gauss divergence theorem. (4 + 6=10)

b) Find the equation of the cone whose vertex is (α, β, γ) and base $ax^2 + by^2 = 1, z = 0$.

5. Find the condition that the plane $lx + my - nz = p$ may touch the paraboloid (10)

$$ax^2 + by^2 = 2cz.$$

6. Trace the conic : $21x^2 - 6xy + 29y^2 + 6x - 58y - 151 = 0$. (10)

*****ALL THE BEST*****